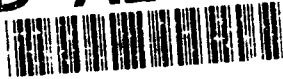


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A COHERENT GRADIENT SENSOR FOR
CRACK TIP DEFORMATION MEASUREMENTS:
ANALYSIS AND EXPERIMENTAL RESULTS

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Abstract

A first order diffraction analysis of an optical interferometer, *Coherent Gradient Sensor* (CGS), for measuring surface gradients is presented. Its applicability in the field of fracture mechanics is demonstrated by quantitatively measuring the gradients of out-of-plane displacements around a crack tip in a three point bend fracture specimen under static loading. This method has potential for the study of deformation fields near a quasi-statically or dynamically growing crack.

1. Introduction

Presently, several optical methods are being used for measuring elastic or plastic crack tip deformations under quasi-static or dynamic loading conditions. Among the commonly used techniques, photoelasticity [1] measures principal stress differences while moiré methods and interferometry [2-4] map in-plane or out-of-plane displacements. In the method of caustics, non-uniform displacement gradients due to crack tip deformations result in the formation of a shadow spot [5,6]. Subsequent interpretation of these optical measurements through an assumed asymptotic field description enables one to evaluate the so-called stress intensity factor (SIF) K_I or the J-integral which are widely used in characterizing fracture behavior of materials.

In most of the above methods [1-4], one often encounters the difficult question of whether the chosen experimental technique provides adequate control over the sensitivity of measurement. This becomes relevant because of the wide range of magnitudes of deformation that may occur near a crack tip. Typically, interferometric methods are preferred for the measurement of elastic deformations while for larger deformations the resulting fringe density often overwhelms the recording capabilities. As a result, geometric moiré methods are used when large deformations exist. However, in fracture studies one often needs a method which can satisfactorily perform in both regimes.

In this paper, we propose an optical interferometer - *coherent gradient sensor* (CGS) to measure in-plane gradients of out-of-plane surface displacements around a crack tip. The method produces high contrast fringes and provides some degree of control on the sensitivity of measurement during quasi-static experiments. In addition, it involves a simple optical set-up and, when compared to other interferometric techniques, it is relatively insensitive to vibrations which makes it a potential candidate for dynamic crack growth applications. Finally, the insensitivity of this method to rigid body motions is highly attractive for solid mechanics applications.

CGS employs the basic principles of the so-called 'moiré deflectometry' used widely

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in a variety of problems by Kafri and his associates [7,8]. However, CGS takes advantage of coherent optics by using wave front division (by means of high density Ronchi rulings) and their subsequent interference. By incorporating an online spatial filtering procedure, one could not only realize high contrast fringes in real time, but also use high density diffraction gratings for the purpose.

In the following, we present a diffraction analysis of the method and experimental evidence to demonstrate its applicability for elastic and elasto-plastic crack tip deformation studies.

2. Experimental Method

2.1 *Experimental Set-up*

In Fig.(1) the schematic of the experimental set up is shown. It consists of a specularly reflective fracture specimen illuminated by a collimated bundle of coherent laser light. Normal incidence is achieved using a beam splitter. The reflected object wave is incident on a pair of high density Ronchi rulings, G_1 and G_2 , separated by a distance Δ . The principal direction of the rulings is coincident with either the x_1 - or x_2 -coordinate axes to obtain $(\partial u_3/\partial x_1)$ or $(\partial u_3/\partial x_2)$, respectively, where $u_3(x_1, x_2)$ denotes the out-of-plane surface displacements. As shown in the schematic, the origin of the coordinate system is located at the crack tip of the specimen. The field distribution on the G_2 plane is spatially filtered by the filtering lens L_1 and its frequency content is displayed on its back focal plane. By locating a filtering aperture around either the ± 1 diffraction orders, the information regarding the displacement gradients is obtained on the image plane of the lens L_2 . It should be pointed out that by using cross gratings instead of line gratings, one could obtain both gradient fields simultaneously by filtering the corresponding diffraction orders on the filter plane. In the following sections, a first order diffraction analysis is performed to demonstrate that the information displayed on the image plane indeed corresponds to gradients of the out-of-plane displacement u_3 .

2.2 Principle

Figure (2) explains the working principle of the CGS interferometer. For the sake of simplicity, and without losing generality, the line gratings are assumed to have a sinusoidal transmittance. For the case of a plane wave reflected from the flat surface of an undeformed specimen and propagating along the optical axis, the incident wave is diffracted into three plane wave fronts E_0 , E_1 and E_{-1} by the first grating G_1 . The magnitude of the angle between the propagation direction of E_0 and $E_{\pm 1}$ is given by the grating equation $\theta = \sin^{-1}(\lambda/p)$, where λ is the wave length and p is the grating pitch. Upon incidence on the second grating G_2 , the wave fronts are further diffracted into $E_{0,0}$, $E_{0,1}$, $E_{1,-1}$, $E_{1,0}$, $E_{1,1}$ etc. These wave fronts which are propagating in distinctly different directions, are then brought to focus at spatially separated diffraction spots on the back focal plane of the filtering lens. The spacing between these diffraction spots is directly proportional to $\sin \theta$ or inversely proportional to the grating pitch p .

Now, consider a plane wave normally incident on a deformed specimen surface. The reflected light bundle incident on G_1 now carries surface displacement gradient information, and is constituted of light rays travelling in arbitrary directions. If a large portion of such a bundle of light has its light rays nearly parallel to the optical axis, each of the diffraction spots will be locally surrounded by a dispersed light field due to the deflected rays. The extent of this dispersion depends on the angle of deflection of the reflected rays. By using a two dimensional aperture at the filtering plane, information existing around one of the spots can be further imaged. This leads to an important but subtle point that should be noted. Since each of the diffraction spots is surrounded by dispersed light containing surface deflection information, overlapping of the information could occur on the filtering plane when the deflection of the ray is sufficiently large (i.e., $\geq (\lambda/2p)$). However, as will be shown in the following sections, this limitation can easily be overcome by the use of higher density gratings.

2.3 Analysis

Consider a specimen whose reflective surface occupies the (x_1, x_2) plane in the undeformed state. Upon deformation the reflector surface can be expressed as,

$$F(x_1, x_2, x_3) = x_3 + f(x_1, x_2) = 0. \quad (1)$$

Consider now, a plane wave which is incident on the specimen along the $-x_3$ direction. The unit surface normal N at a generic point $O(x_1, x_2)$ is given by,

$$N = \frac{\nabla F}{|\nabla F|} = \frac{f_{,1}e_1 + f_{,2}e_2 + e_3}{\sqrt{1 + f_{,1}^2 + f_{,2}^2}}, \quad (2)$$

where e_i denote the unit vectors of the Cartesian coordinate system (see Fig.(3)) and $f_{,\alpha}$ implies differentiation with respect to x_α . Let d be the unit vector along the reflected ray whose direction cosines are α_0, β_0 and γ_0 . From the law of reflection, the coplanar unit vectors d, N and e_3 are related by $d \cdot N = e_3 \cdot N$. This leads to

$$d = (2e_3 \cdot N)N - e_3. \quad (3)$$

By substituting Eqn.(2) in (3),

$$d = (\alpha_0 e_1 + \beta_0 e_2 + \gamma_0 e_3) = \frac{2(f_{,1}e_1 + f_{,2}e_2 + e_3)}{(1 + f_{,1}^2 + f_{,2}^2)} - e_3. \quad (4)$$

Thus, the direction cosines of d can be related to the gradients of the function f by

$$\alpha_0 = \frac{2f_{,1}}{(1 + f_{,1}^2 + f_{,2}^2)}, \quad \beta_0 = \frac{2f_{,2}}{(1 + f_{,1}^2 + f_{,2}^2)}, \quad \gamma_0 = \frac{(1 - f_{,1}^2 - f_{,2}^2)}{(1 + f_{,1}^2 + f_{,2}^2)}. \quad (5)$$

The ray along d upon incidence on the grating G_1 is split into rays propagating along $d_0, d_{\pm 1}$ whose amplitudes $E_0(x'), E_1(x')$ and $E_{-1}(x')$ can be represented by,

$$E_0(x') = a_0 \exp[ikd_0 \cdot x'], \quad E_1(x') = a_1 \exp[ikd_1 \cdot x'], \quad E_{-1}(x') = a_{-1} \exp[ikd_{-1} \cdot x'], \quad (6)$$

where a_0 and a_1 are constants and the wave number $k = 2\pi/\lambda$. Due to diffraction by the sinusoidal grating G_1 , the propagation directions of the resulting wave fronts are related by,

$$\mathbf{d}_{\pm 1} = \Omega_{\pm 1} \mathbf{d}_0, \quad (7)$$

where $\Omega_{\pm 1}$ are rotation tensors whose matrices of components are given by,

$$[\Omega_{\pm 1}]_{ij} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & \pm \sin \theta \\ 0 & \mp \sin \theta & \cos \theta \end{pmatrix}, \quad (8)$$

and $\theta = \sin^{-1}(\lambda/p)$. From Eqns.(7) and (4) we find

$$\mathbf{d}_{\pm 1} = [\alpha_0 \mathbf{e}_1 + (\beta_0 \cos \theta \pm \gamma_0 \sin \theta) \mathbf{e}_2 + (\gamma_0 \cos \theta \mp \beta_0 \sin \theta) \mathbf{e}_3]. \quad (9)$$

Now, with reference to Fig.(3), on plane G_2 we have

$$E_0(O'B) = a_0 \exp[ik \mathbf{d}_0 \cdot O'B]. \quad (10)$$

In addition, since $|O'B| \mathbf{d}_0 \cdot \mathbf{e}_3 = |O'B| \gamma_0 = \Delta$, one finds that $|O'B| = (\Delta/\gamma_0)$. Hence,

$$E_0(O'B) = a_0 \exp \left[ik \left(\frac{\Delta}{\gamma_0} \right) \right] \quad (11)$$

In like manner,

$$|O'A| \mathbf{d}_1 \cdot \mathbf{e}_3 = |O'A| (\gamma_0 \cos \theta - \beta_0 \sin \theta) = \Delta, \quad (12)$$

$$|O'B'| \mathbf{d}_{-1} \cdot \mathbf{e}_3 = |O'B'| (\gamma_0 \cos \theta + \beta_0 \sin \theta) = \Delta, \quad (13)$$

and thus,

$$E_1(O'A) = a_1 \exp[ik \mathbf{d}_1 \cdot O'A] = a_1 \exp \left[ik \frac{\Delta}{(\gamma_0 \cos \theta - \beta_0 \sin \theta)} \right], \quad (14)$$

$$E_{-1}(O'B') = a_1 \exp[ik \mathbf{d}_{-1} \cdot O'B'] = a_1 \exp \left[ik \frac{\Delta}{(\gamma_0 \cos \theta + \beta_0 \sin \theta)} \right]. \quad (15)$$

2.4 Spatial Filtering

Let the field distribution on the G_2 plane due to the amplitudes E_0 , E_1 and E_{-1} be $H(x''_1, x''_2)$ where the double primed coordinate system is obtained by the translation of (x_1, x_2) coordinate system. Further, let the transmission function of the sinusoidal grating G_2 , whose principal direction is parallel to the x''_2 -axis, be

$$t(x''_1, x''_2) = b \left(1 + \cos \frac{2\pi x''_2}{p} \right), \quad (16)$$

where b is a constant. Then the field distribution immediately after G_2 is

$$R(x''_1, x''_2) = b \left(1 + \cos \frac{2\pi x''_2}{p} \right) [E_0 + E_1 + E_{-1}] = b \left(1 + \cos \frac{2\pi x''_2}{p} \right) H(x''_1, x''_2). \quad (17)$$

The lens L_1 performs a Fourier transform of the above field distribution. Thus, the amplitude distribution on the filtering plane is

$$\mathcal{F}[R(x''_1, x''_2)] = b \left[\delta(\omega_1, \omega_2) + \frac{1}{2} \delta(\omega_1, \omega_2 - \frac{1}{p}) + \frac{1}{2} \delta(\omega_1, \omega_2 + \frac{1}{p}) \right] \star \mathcal{F}[H(x''_1, x''_2)], \quad (18)$$

where $\omega_i = x''_i / \lambda f_{L1}$ denote the in-plane coordinates of the filtering plane, f_{L1} is the focal length of the filtering lens L_1 , δ is the Dirac function, and \star denotes convolution. It is clear from the above expression that the information regarding the surface deflections (direction cosines of d), which is contained in $H(x''_1, x''_2)$, can be filtered out by locating suitably an aperture centered at $\omega_2 = \pm(1/p)$ on the filtering plane. Imaging this information through the second lens L_2 is equivalent to performing a Fourier transform on the filtered field which gives us the amplitude distribution on the image plane as,

$$E_{im} = \mathcal{F} \left[\mathcal{F}(H(x''_1, x''_2)) \star \frac{b}{2} \delta(\omega_1, \omega_2 \pm \frac{1}{p}) \right] = \frac{b}{2} H(-x''_1, -x''_2) \exp \left(\pm i \frac{2\pi x''_2}{p} \right). \quad (19)$$

The intensity distribution on the image plane can now be calculated as,

$$\begin{aligned} I_{im} = E_{im} E_{im}^* &= b_0^2 + 2b_1^2 + 2b_0 b_1 \cos \left\{ k\Delta \left[\frac{\gamma_0(\cos \theta - 1) - \beta_0 \sin \theta}{\gamma_0(\gamma_0 \cos \theta - \beta_0 \sin \theta)} \right] \right\} \\ &+ 2b_0 b_1 \cos \left\{ k\Delta \left[\frac{\gamma_0(\cos \theta - 1) + \beta_0 \sin \theta}{\gamma_0(\gamma_0 \cos \theta + \beta_0 \sin \theta)} \right] \right\} \\ &+ 2b_1^2 \cos \left\{ k\Delta \left[\frac{2\beta_0 \sin \theta}{(\gamma_0^2 \cos^2 \theta - \beta_0^2 \sin^2 \theta)} \right] \right\}, \end{aligned} \quad (20)$$

where b_0 and b_1 are constants and E_{im}^* is the complex conjugate of E_{im} . Under small θ approximation the above equation reduces to

$$I_{im} = b_0^2 + 2b_1^2 + 4b_0b_1 \cos\left(\frac{k\Delta\beta_0\theta}{\gamma_0^2}\right) + 2b_1^2 \cos\left(\frac{2k\Delta\beta_0\theta}{\gamma_0^2}\right). \quad (21)$$

Thus, I_{im} denotes an intensity variation on the image plane whose maxima occur when

$$\frac{k\Delta\beta_0\theta}{\gamma_0^2} = 2n\pi, \quad n = 0, \pm 1, \pm 2, \dots \quad (22)$$

From Eqn.(5) the direction cosines α_0 , β_0 and γ_0 are related to the gradients of the function f . Then, the above equation can be rewritten as,

$$k\Delta\theta \left[2f_{,2} \left(\frac{1 + |\nabla f|^2}{(1 - |\nabla f|^2)^2} \right) \right] = 2n\pi. \quad (23)$$

When $|\nabla f|^2 \ll 1$, Eqn.(23) becomes,

$$f_{,2} \approx \left(\frac{np}{2\Delta} \right) \quad n = 0, \pm 1, \pm 2, \dots \quad (24)$$

where the fact that $\theta \approx (\lambda/p)$ and $k = 2\pi/\lambda$ are made use of. Similarly, when the gratings are oriented with their principal direction coinciding with the x_1 -axis,

$$f_{,1} \approx \left(\frac{mp}{2\Delta} \right) \quad m = 0, \pm 1, \pm 2, \dots \quad (25)$$

Thus, Eqns.(24) and (25) are the governing equations for the method of CGS. It should be noted that these equations are similar in form to those of moiré deflectometry [8] and reflection moiré methods [9] based on geometric optics. It is clear from the above two equations that the sensitivity of the method could be increased by either increasing the grating separation distance Δ or decreasing the grating pitch p . However, for small Δ , one needs to exercise caution in order to avoid the formation of gap moiré fringes when the lens system is arranged such that the object surface is in focus. Another interesting point to be noted is that Eqn.(21) provides an explanation for the high contrast of the fringes obtained in this method. Under the assumption that the gratings used have sinusoidal transmittance, the expression for intensity distribution I_{im} indicates a fringe sharpening effect due to the existence of higher frequency term $(2\Delta\beta_0\theta/\gamma_0^2)$. The use of

Ronchi gratings with nearly rectangular transmittance leads to further fringe sharpening due to the existence of several of such higher order frequencies.

3. Experimental Results

Two experiments are performed to demonstrate the applicability of CGS in solid mechanics in general and fracture mechanics in particular. First, the gradients of a known function f were used to test the reliability of the measurements. For this purpose, a spherical wave front was generated using a convex lens of focal length $f_l=546$ mm. Line gratings of density 40 lines per mm were oriented with their principal direction coinciding with the x_2 -axis and were separated by a distance of $\Delta=22$ mm to produce fringes that are shown in Fig.(4). The fringe spacing (x_2/n) corresponding to the gradients in the x_2 - direction namely, $f_{,2}$ measured from the fringe pattern is 0.66 mm/fringe. The spherical wave front emerging from the convex lens can be described by,

$$f(x_1, x_2) = \frac{x_1^2 + x_2^2}{2f_l}, \quad (26)$$

and hence (in transmission),

$$\beta_0 = f_{,2} = \left(\frac{x_2}{f_l} \right) = \frac{np}{\Delta}, \quad (27)$$

which corresponds to straight line fringes as shown in the figure. For the experimental parameters used in this demonstration, the fringe density expected from the above equations is 0.63 mm/fringe which is in good agreement with the experimental measurements.

Secondly, CGS was used to obtain gradients of the out-of-plane displacement $u_3(x_1, x_2)$ ($= -f(x_1, x_2)$) around a deformed crack tip in a three point bend fracture specimen made of AISI 4340 steel. The dimensions of the specimen and the experimental set up are shown in Figs.(5) and (6). The specimen has an electro-discharge machined notch which is 25 μ m wide and 30 mm deep through a 10 mm thick plate. The specimen was heat treated to have a yield stress of 1350 MPa. One of the surfaces of the specimen was lapped and polished to obtain a flat reflective test surface. The specimen was statically loaded in a

hydraulic loading frame in displacement control mode. The load and the load point displacements were measured during the test. The optical set up has two Ronchi rulings of 40 lines per mm density and are separated by a distance (Δ) of 21 mm giving a sensitivity of measurement 6.05×10^{-4} rad/fringe. In Fig.(7) fringe patterns representing contours of constant $(\partial u_3/\partial x_1)$ and $(\partial u_3/\partial x_2)$ corresponding to three load levels $P/P_0=0.38, 0.61, 0.71$ are shown where P_0 is the plane stress limit load for the specimen. For the lowest load level of the three patterns shown (Fig.(7a)), the near tip out-of-plane displacement field was assumed to be given by the linear elastic, asymptotic, plane stress expression,

$$\begin{aligned} f(r, \phi) = -u_3(r, \phi) &= \frac{\nu h}{2E} [\sigma_{11}(r, \phi) + \sigma_{22}(r, \phi)] \\ &\approx \frac{\nu h K_I}{E \sqrt{2\pi r}} \cos(\phi/2) + \left(\frac{\nu h}{2E} \right) \sigma_{11}^0 + o(1), \quad \text{as } r \rightarrow 0, \end{aligned} \quad (28)$$

where $r = \sqrt{x_1^2 + x_2^2}$, $\phi = \tan^{-1}(x_2/x_1)$, h is the specimen thickness, E is Young's modulus, ν is Poisson's ratio, σ_{11}^0 is the constant term in the asymptotic expansion for the stresses, and K_I is the mode-I stress intensity factor to be determined by CGS.

By using Eqns.(24) and (25), the stress intensity factor can now be obtained from the fringe pattern, Fig.(7a), through:

$$(K_I)_{CGS} = \frac{2E\sqrt{2\pi}r^{3/2}}{\nu h \cos(3\phi/2)} \cdot \left(\frac{mp}{2\Delta} \right), \quad m = 0, \pm 1, \pm 2, \dots \quad (29)$$

In the above expression, m is the fringe order and $(K_I)_{CGS}$ denotes the experimentally obtained value for the stress intensity factor. Note that the constant term σ_{11}^0 does not appear in Eqn.(29) because the measurements are sensitive to surface gradients only. $(K_I)_{CGS}$ can now be computed from different fringes corresponding to different (r, ϕ) pairs. If the out-of-plane displacement field of the specimen surface is indeed given by Eqn.(28), the experimentally obtained $(K_I)_{CGS}$ should be independent of the location of measurement (choice of r, ϕ pairs in Eqn.(29)). In such a case, $(K_I)_{CGS}$ should agree with the stress intensity factor $(K_I)_{2D}$ obtained from boundary value measurements by means of a two dimensional analysis [10].

However, near the crack tip three dimensional effects are expected to violate the plane stress assumption which leads to Eqn.(28). Indeed, the experimental results reported by

Rosakis and Ravi-Chandar [12] and supported by the analytical investigations of Yang and Freund [11] have shown that Eqn.(28) is a good description of the surface out-of-plane displacements only for radial distances greater than $0.5h$. This behavior is also evident from the current experimental results displayed in Fig.(8). Here, $(K_I)_{2D}$ is obtained through the boundary load and the results compiled in Ref.[10]. $(K_I)_{CGS}$ is obtained from fringes at different radial distances along the $\phi = 0$ line by using Eqn.(29). It is clear from the figure that the measured value of $(K_I)_{CGS}$ is in good agreement with $(K_I)_{2D}$ for $(r/h) > 0.5$. However, for $(r/h) < 0.5$, a marked under estimation of the inferred stress intensity factor is observed. This is consistent with the results shown in Figs.(5) and (6) of Ref.[12] which are obtained by using the optical method of caustics. This is to be expected since both caustics and CGS rely on surface out-of-plane displacement gradients.

The fringe patterns in Figs.(7b,c) correspond to substantial near tip plastic deformations and as such the use of Eqns.(28) and (29) is inappropriate. Direct comparison of the experimentally obtained displacement fields with a three dimensional elastic-plastic finite element analysis of the specimen is underway.

4. Conclusions

This paper provides a detailed diffraction analysis of the proposed interferometer, Coherent Gradient Sensor. The analysis indicates that the resulting interference fringes represent contours of constant surface gradients. Although the method bears similarities in its operating principle with moiré deflectometry [8], it has additional advantages because it uses coherent optics. Unlike moiré deflectometry, which is limited by diffraction effects, this method utilizes such effects by making use of high density gratings and spatial filtering procedure. Also, spatial filtering enhances the contrast and sharpness of the fringes.

The feasibility of CGS as a means of quantifying crack tip deformation fields has

been demonstrated in the elastic and plastic regimes. Simplicity of the optical set up, sharp and high contrast fringes and limited loss of light intensity make CGS a suitable candidate for dynamic crack initiation and propagation studies. Its relative insensitivity to laboratory vibrations comes as an additional advantage.

Acknowledgments

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Figure Captions

Figure 1. Schematic of the Experimental Set-up for CGS

Figure 2. Working Principle for CGS

Figure 3. Diffraction of a Generic Ray in the CGS

Figure 4. Contours of Constant f_2 for a Spherical Wave Front

Figure 5. Specimen Geometry of the 3-point Bend Fracture Specimen

Figure 6. Experimental Arrangement for Fracture Experiment Using CGS

Figure 7a. Contours of $(\partial u_3/\partial x_1)$ and $(\partial u_3/\partial x_2)$ for $(P/P_0)=0.38$

Figure 7b. Contours of $(\partial u_3/\partial x_1)$ and $(\partial u_3/\partial x_2)$ for $(P/P_0)=0.61$

Figure 7c. Contours of $(\partial u_3/\partial x_1)$ and $(\partial u_3/\partial x_2)$ for $(P/P_0)=0.71$

Figure 8. Experimental Results from $(\partial u_3/\partial x_1)$ fringes along $(r, \phi = 0)$ line for $(P/P_0)=0.38$

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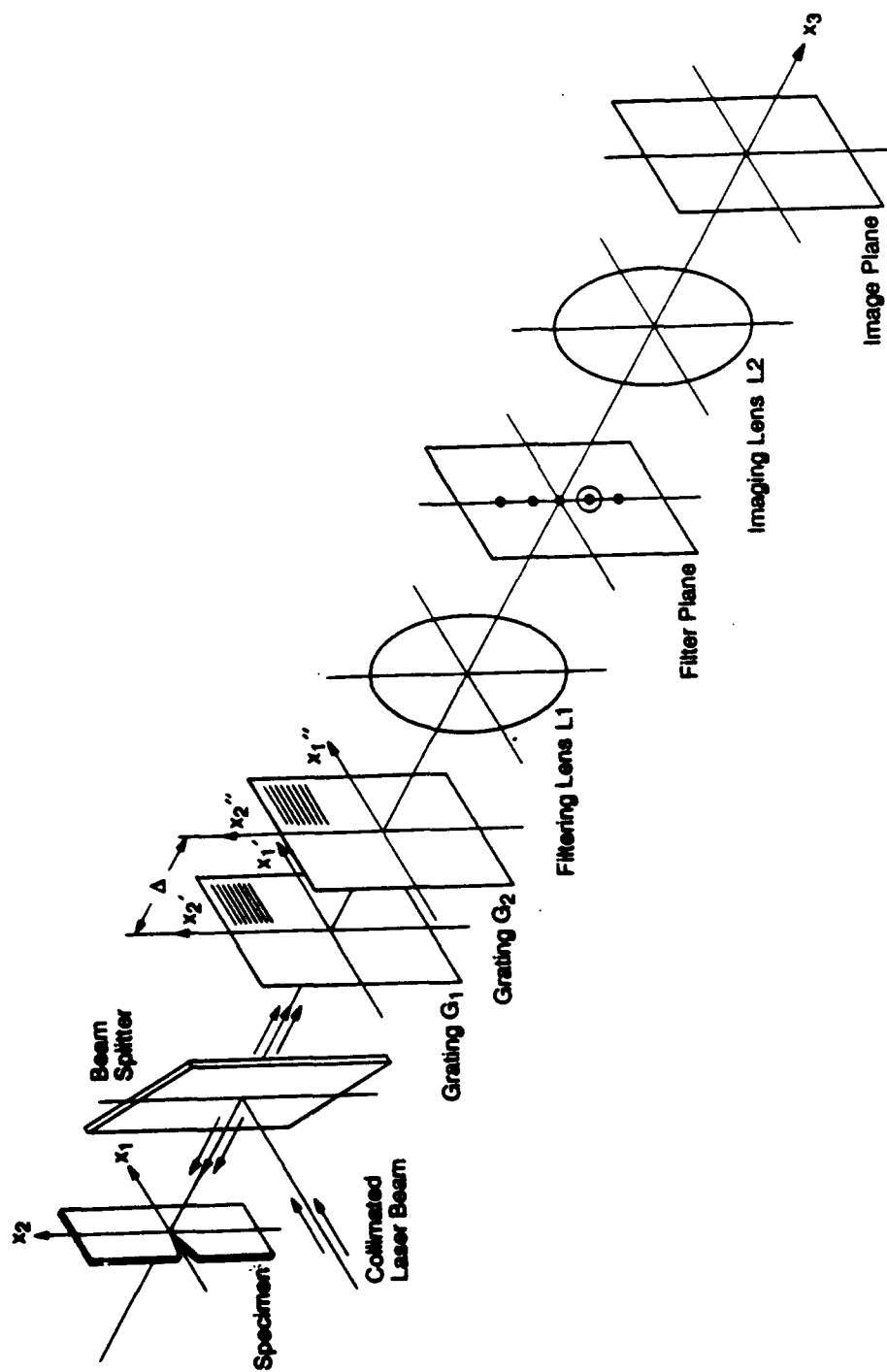


Figure 1. Schematic of the Experimental Set-up for CGS

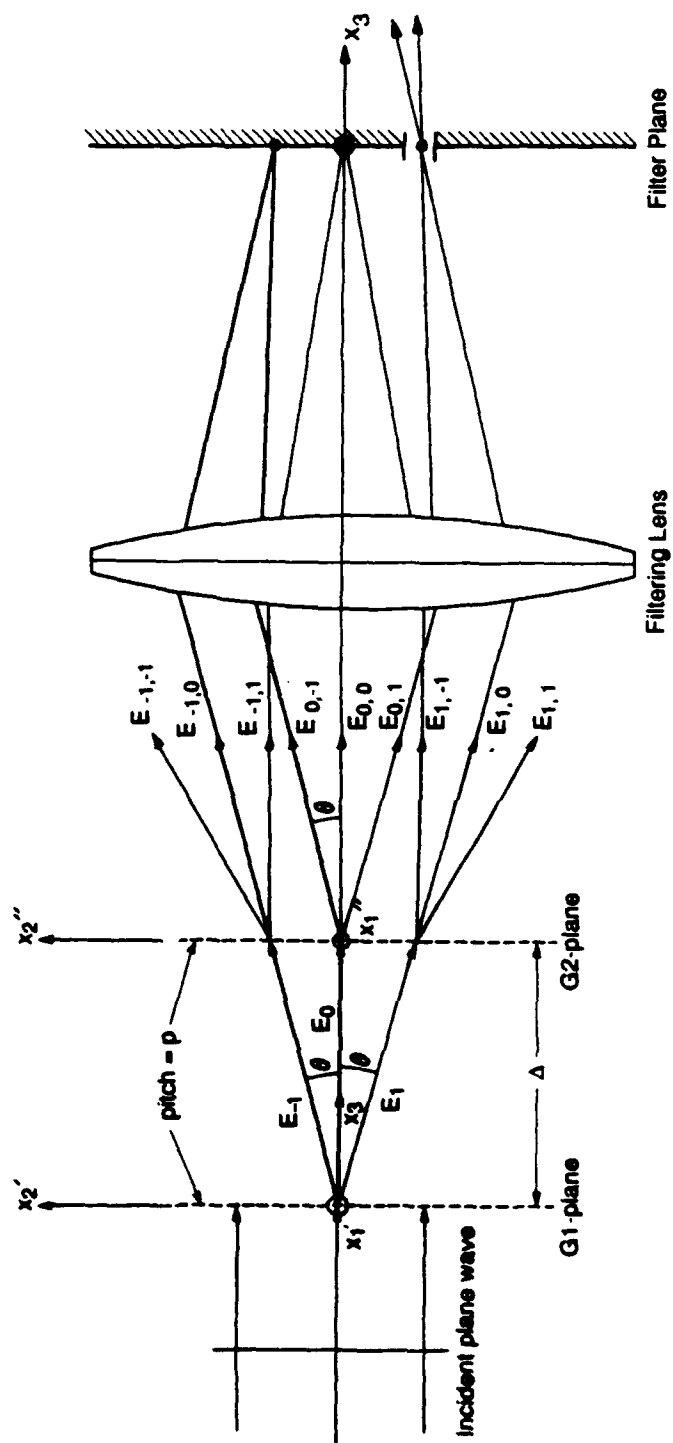


Figure 2. Working Principle for CGS

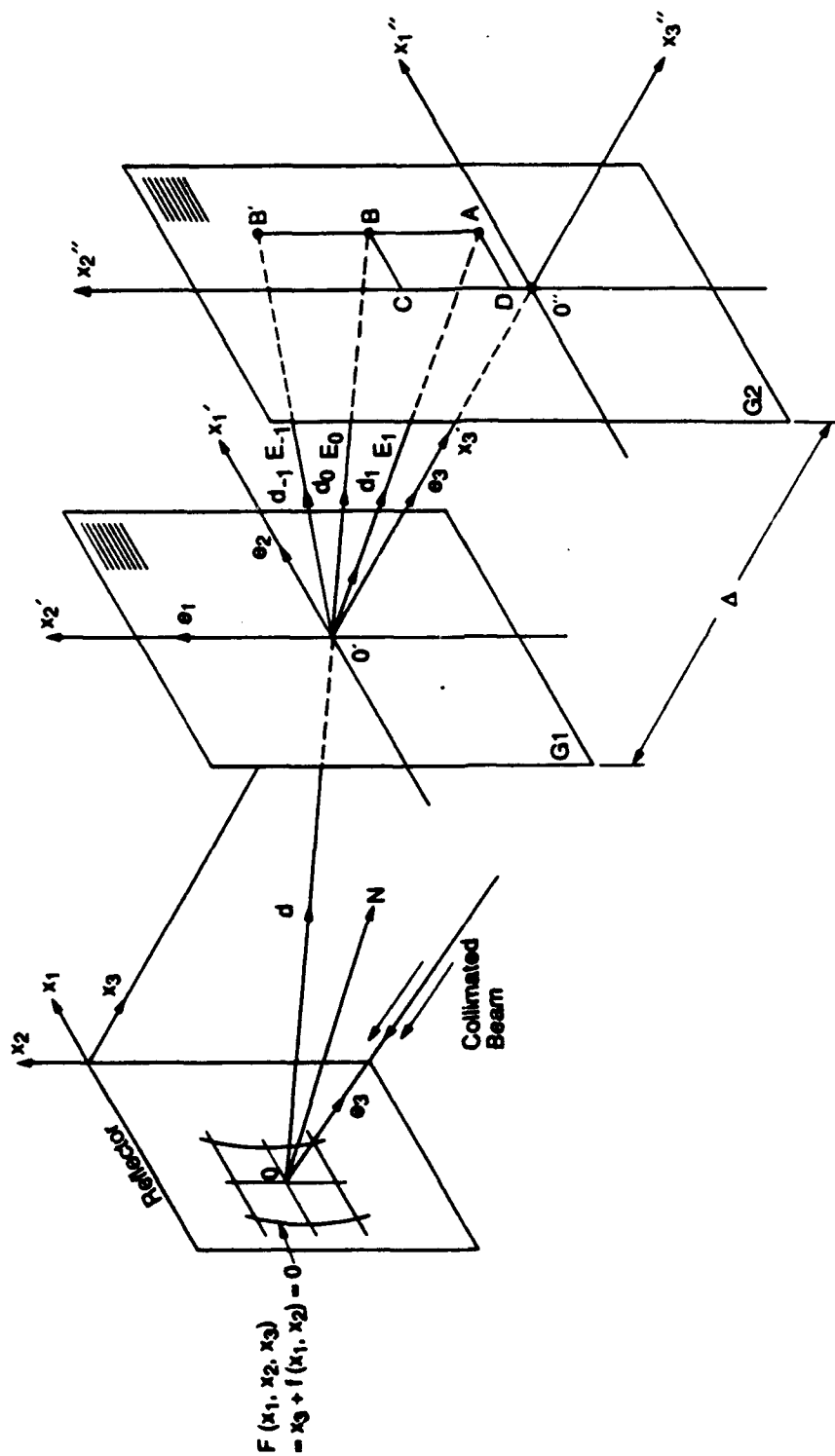


Figure 3. Diffraction of a Generic Ray in the CGS

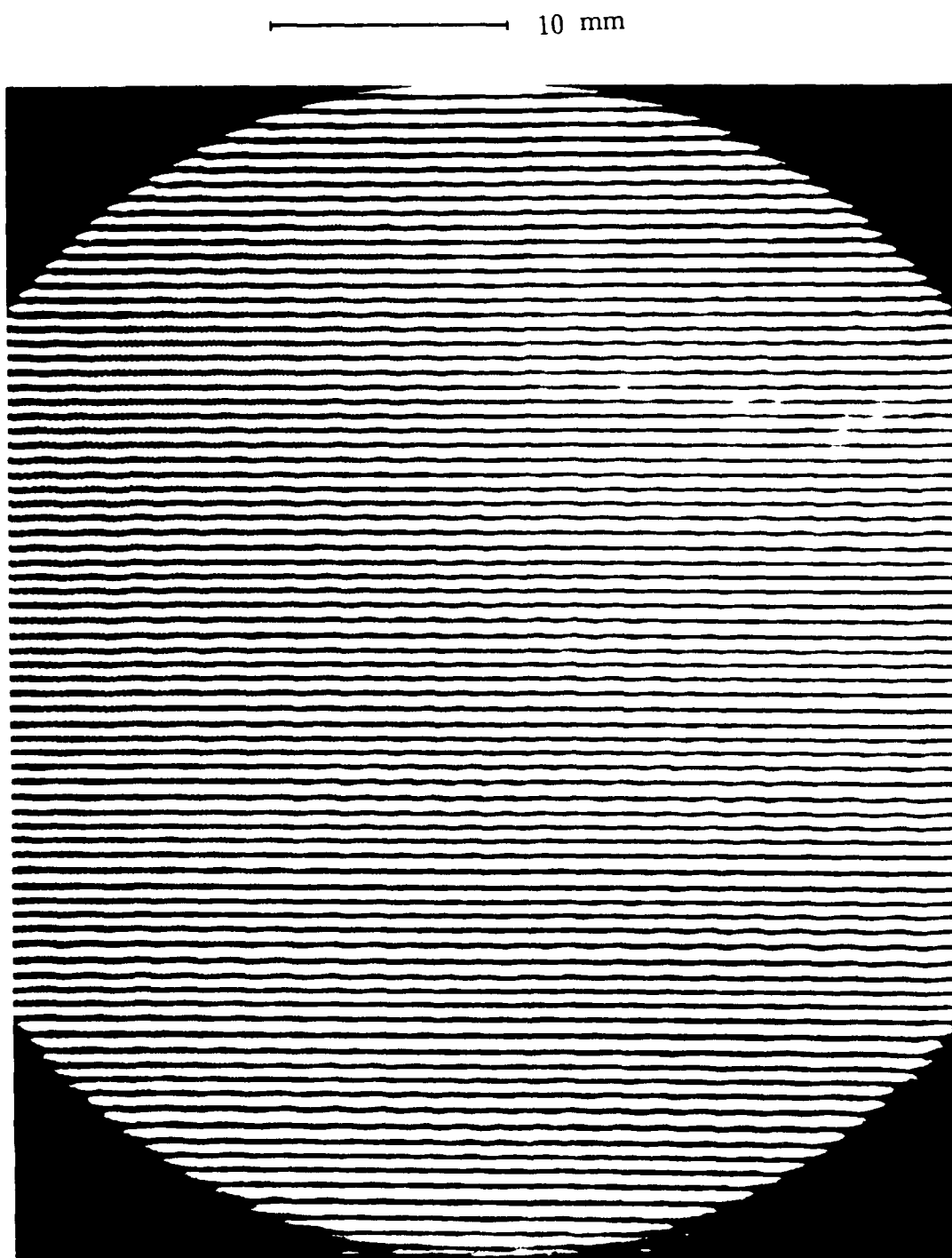


Figure 4. Contours of Constant f_2 for a Spherical Wave Front

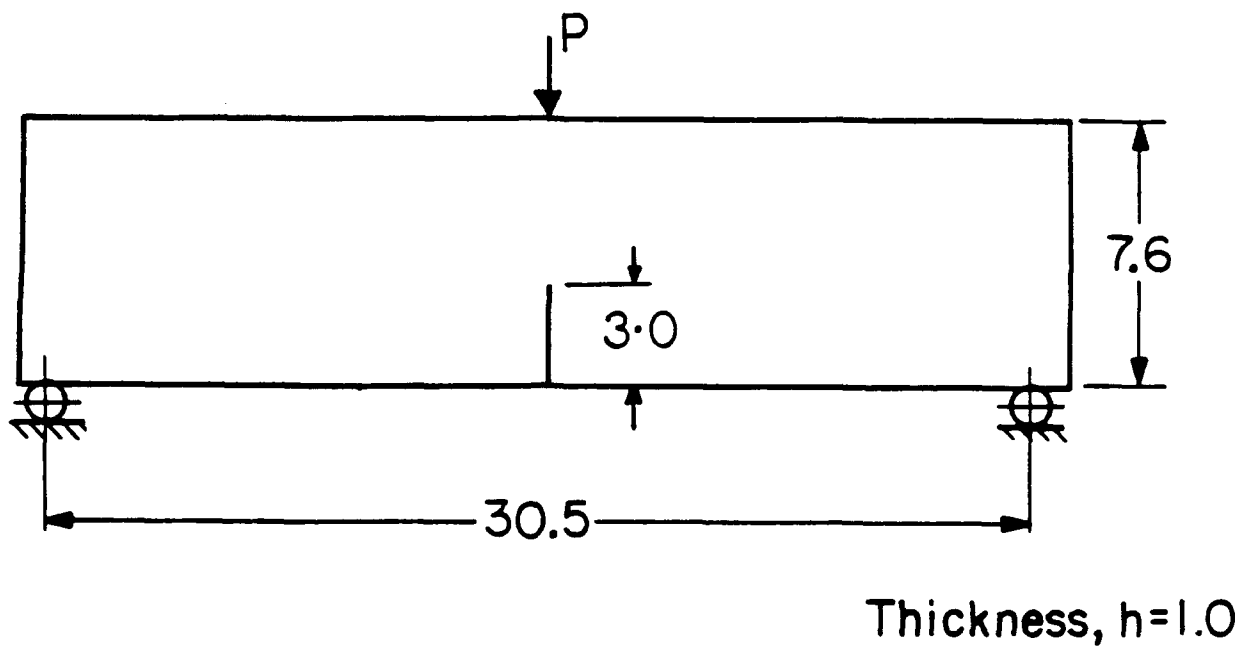


Figure 5. Specimen Geometry of the 3-point Bend Fracture Specimen
All dimensions are in cm.

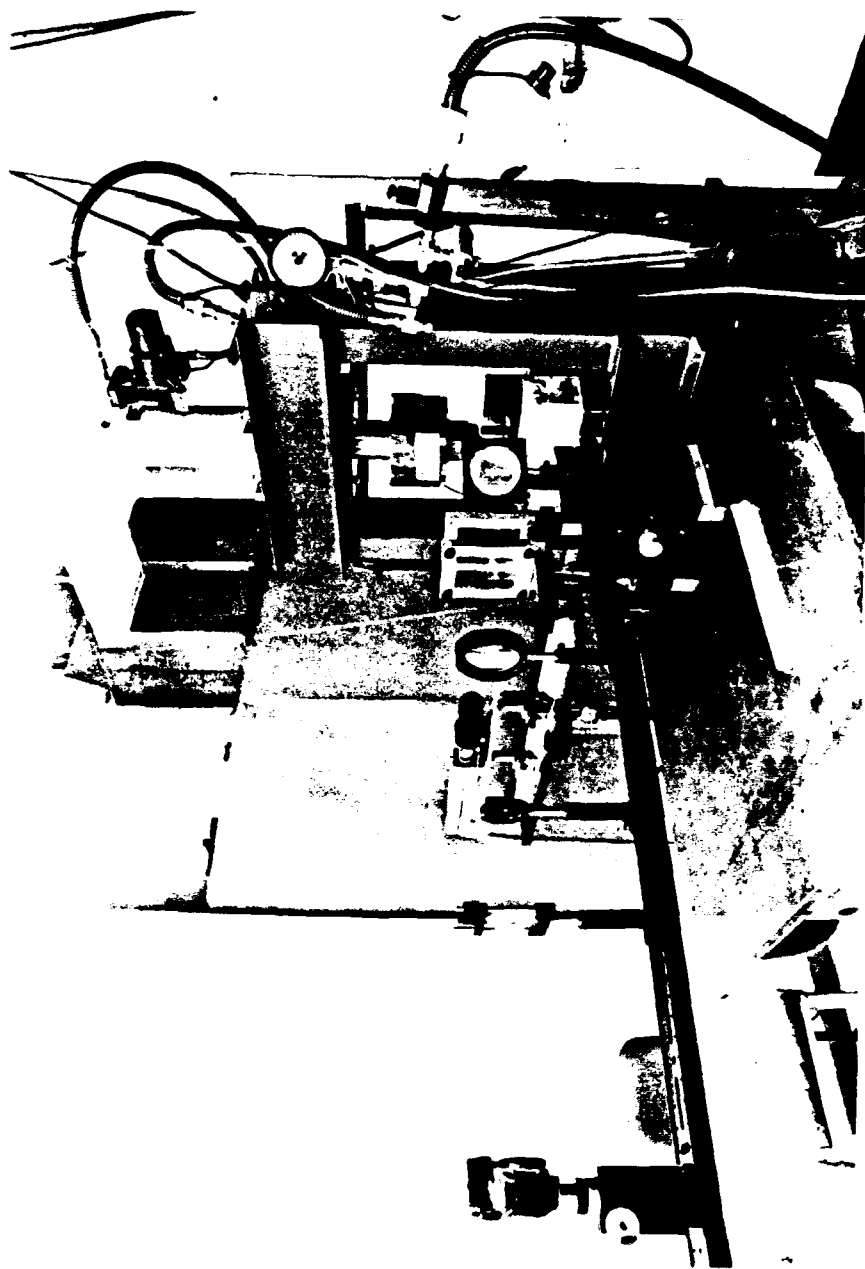


Figure 6. Experimental Arrangement for Fracture Experiment Using CGS

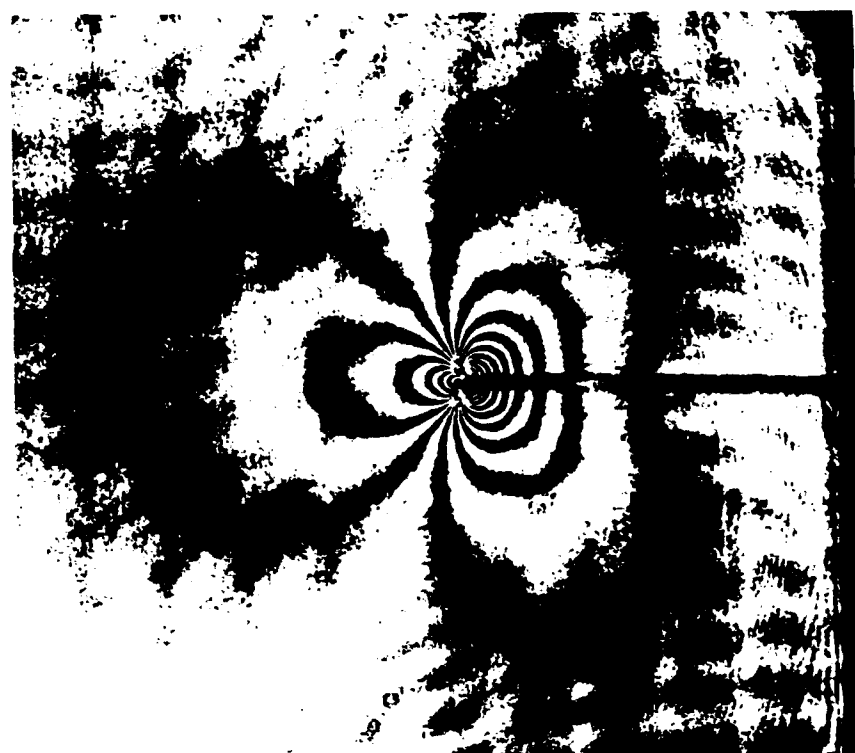


Figure 7a. Contours of $(\partial u_3 / \partial x_1)$ and $(\partial u_3 / \partial x_2)$ for $(P/P_0)=0.38$

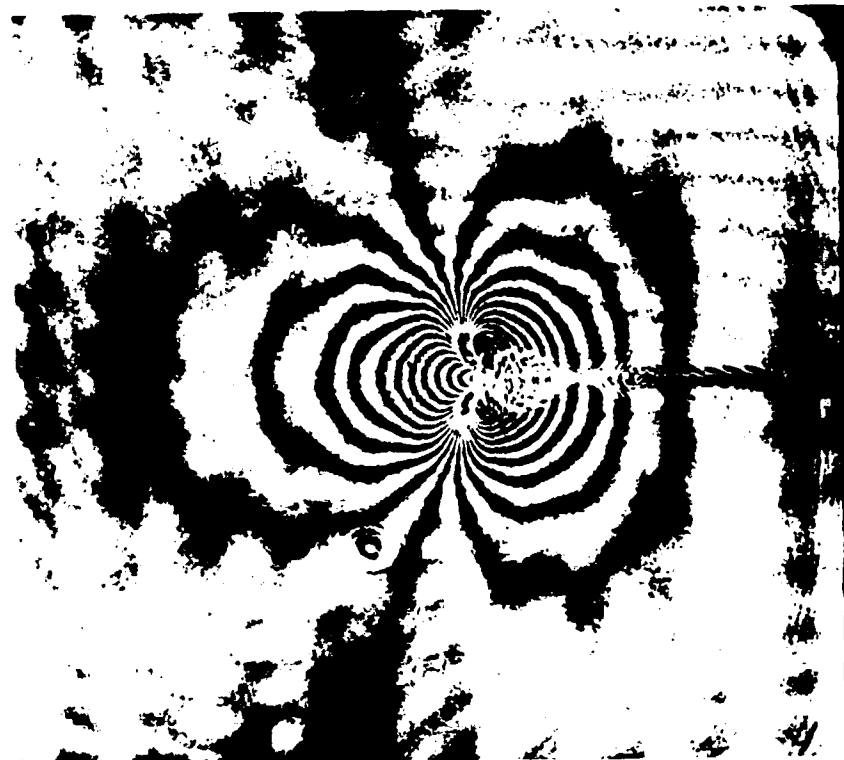


Figure 7b. Contours of $(\partial u_3 / \partial x_1)$ and $(\partial u_3 / \partial x_2)$ for $(P/P_0) = 0.61$

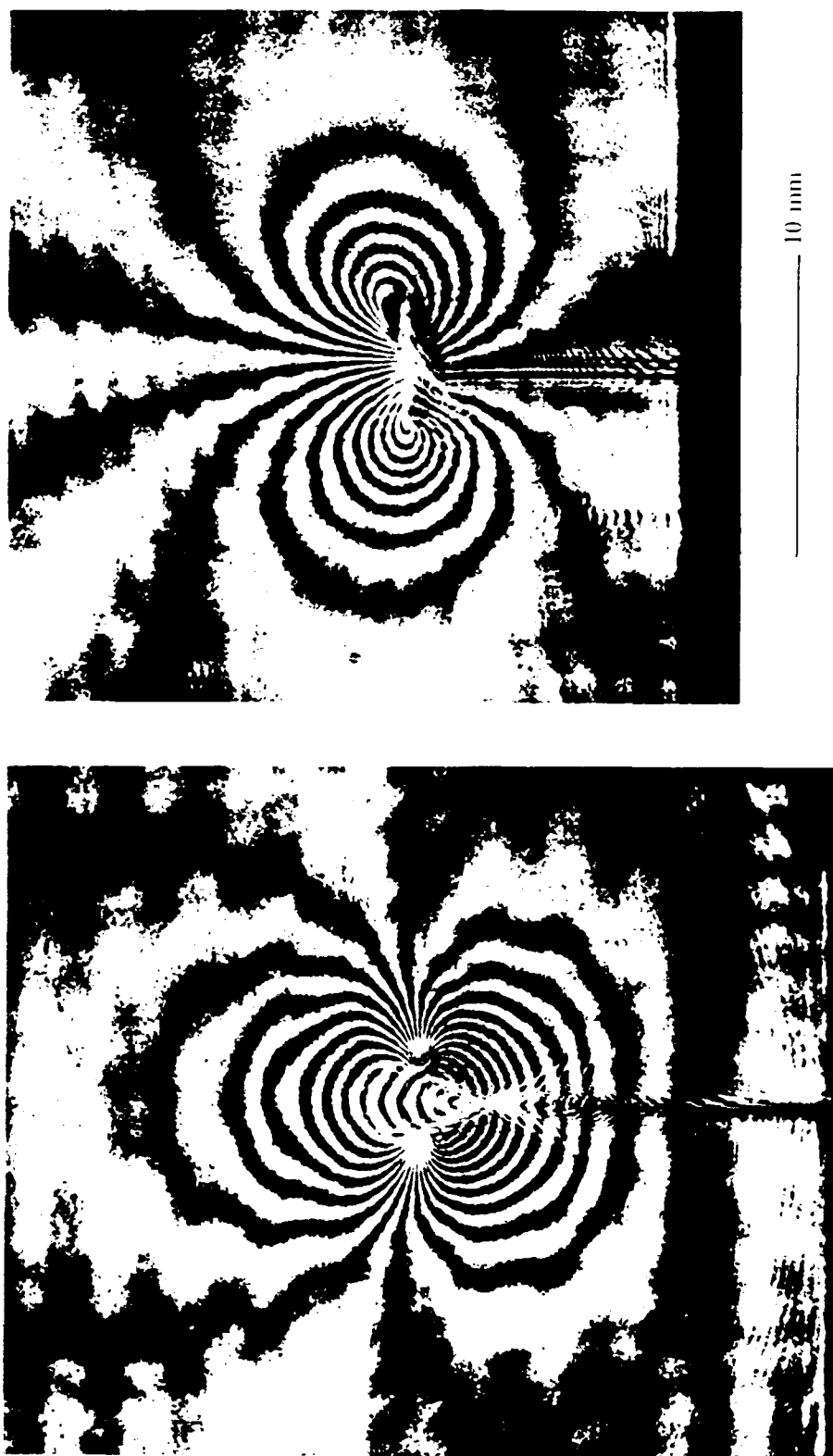


Figure 7c. Contours of $(\partial u_3/\partial x_1)$ and $(\partial u_3/\partial x_2)$ for $(P/P_0)=0.71$

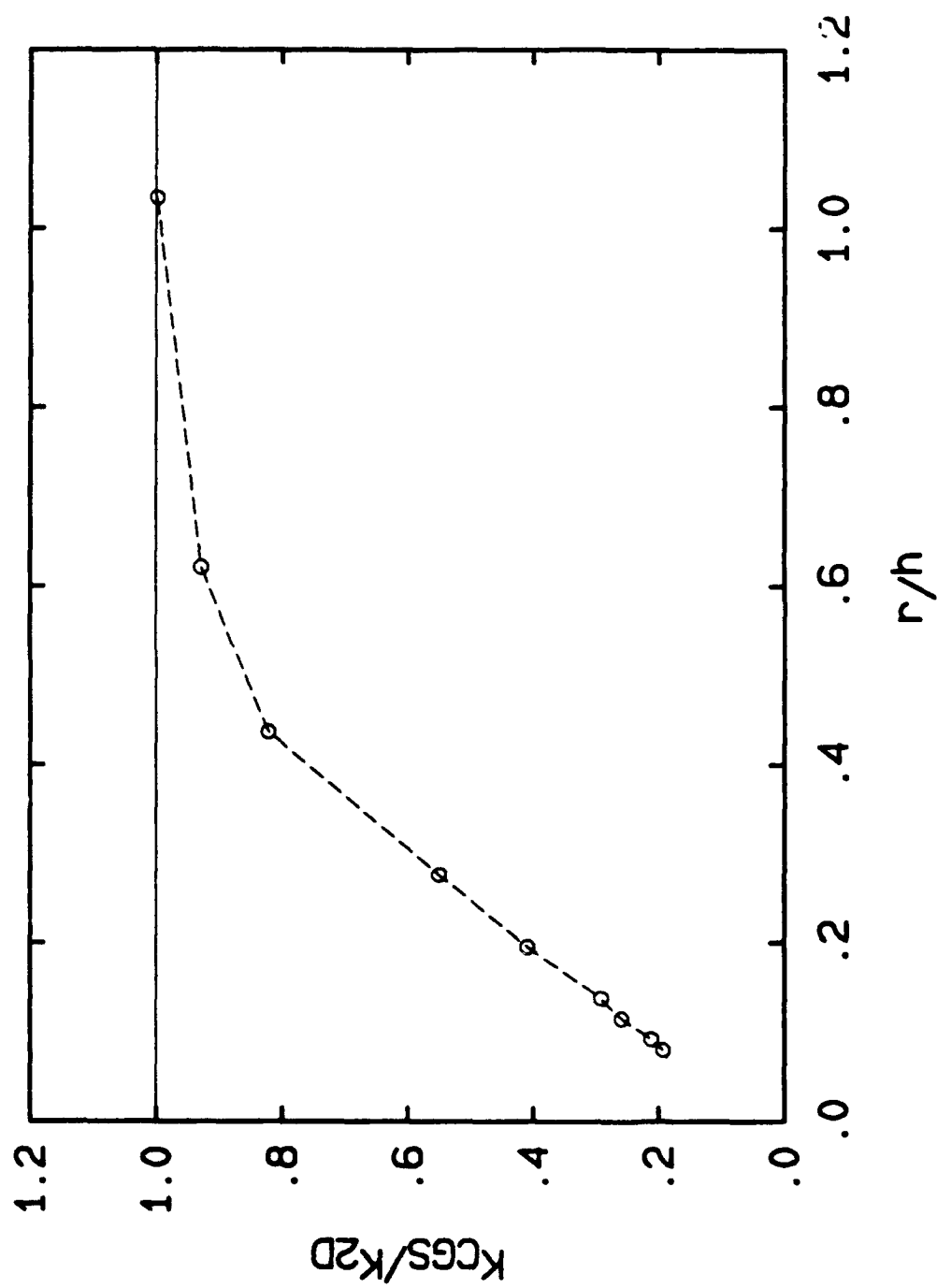


Figure 8. Experimental Results from $(\partial u_3 / \partial x_1)$ fringes along $(r, \phi = 0)$ line for $(P/P_0) = 0.38$

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20. ABSTRACT (Continue on reverse side if necessary and identify by block number) A first order diffraction analysis of an optical interferometer, <u>Coherent Gradient Sensor</u> (CGS), for measuring surface gradients is presented. Its applicability in the field of fracture mechanics is demonstrated by quantitatively measuring the gradients of out-of-plane displacements around a crack tip in a three point bend fracture specimen under static loading. This method has potential for the study of deformation fields near a quasi-statically or dynamically growing crack.		